MPI for Scalable Computing

Tutorial at ATPESC, July 2020
Latest slides and code examples are available at

https://anl.box.com/v/atpesc2020-mpi-tutorial

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About the Speakers

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- **Rajeev Thakur**: Deputy Division Director, Argonne National Laboratory

All of us are deeply involved in MPI standardization (in the MPI Forum) and in MPI implementation
The MPI Part of ATPESC

- We assume everyone already has some MPI experience
- We will focus more on understanding MPI concepts than on coding details
- Emphasis will be on issues affecting scalability and performance
- There will be code walkthroughs and hands-on exercises
Outline

- **Morning**
  - Introduction to MPI and this tutorial
  - Avoiding unnecessary synchronization
  - Topics in collective communication
  - Stencil example and hands-on exercises
  - Minimizing data motion using MPI derived datatypes
  - Begin RMA

- **Afternoon**
  - One-sided communication (or remote memory access)
  - Hands-on exercises
  - Hybrid programming
    - MPI + threads
    - MPI + shared-memory
    - MPI + GPUs
  - Hands-on exercises
What is MPI?

- MPI: Message Passing Interface
  - The MPI Forum organized in 1992 with broad participation by:
    - Vendors: IBM, Intel, TMC, SGI, Convex, Meiko
    - Portability library writers: PVM, p4
    - Users: application scientists and library writers
    - MPI-1 finished in 18 months
  - Incorporates the best ideas in a “standard” way
    - Each function takes fixed arguments
    - Each function has fixed semantics
      - Standardizes what the MPI implementation provides and what the application can and cannot expect
      - Each system can implement it differently as long as the semantics match

- MPI is not...
  - a language or compiler specification
  - a specific implementation or product
MPI-1

- MPI-1 supports the classical message-passing programming model: basic point-to-point communication, collectives, datatypes, etc
- MPI-1 was defined (1994) by a broadly based group of parallel computer vendors, computer scientists, and applications developers.
  - 2-year intensive process
- Implementations appeared quickly and now MPI is taken for granted as vendor-supported software on any parallel machine.
- Free, portable implementations exist for clusters and other environments (MPICH, Open MPI)
Following MPI Standards

- MPI-2 was released in 1997
  - Several additional features including MPI + threads, MPI-I/O, remote memory access functionality and many others
- MPI-2.1 (2008) and MPI-2.2 (2009) were released with some corrections to the standard and small features
- MPI-3 (2012) added several new features to MPI
- MPI-3.1 (2015) is the latest version of the standard with minor corrections and features
- The Standard itself:
  - at http://www.mpi-forum.org
  - All MPI official releases, in both postscript and HTML
- Other information on Web:
  - at http://www.mcs.anl.gov/mpi
  - pointers to lots of material including tutorials, a FAQ, other MPI pages
Overview of New Features in MPI-3

- Major new features
  - Nonblocking collectives
  - Neighborhood collectives
  - Improved one-sided communication interface
  - Tools interface
  - Fortran 2008 bindings

- Other new features
  - Matching Probe and Recv for thread-safe probe and receive
  - Noncollective communicator creation function
  - “const” correct C bindings
  - Comm_split_type function
  - Nonblocking Comm_dup
  - Type_create_hindexed_block function

- C++ bindings removed

- Previously deprecated functions removed

- MPI 3.1 added nonblocking collective I/O functions
## Status of MPI-3.1 Implementations

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<th>MVAPICH</th>
<th>Open MPI</th>
<th>Cray</th>
<th>Thinking</th>
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<th>IBM</th>
<th>HP/EG</th>
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- Platform-specific restrictions might apply to the supported features
- Release dates are estimates; subject to change at any time

"✓" indicates no publicly announced plan to implement/support that feature

1 Open Source but unsupported
2 No MPI_T variables exposed
* Under development
(*) Partly done
Important considerations while using MPI

- All parallelism is explicit: the programmer is responsible for correctly identifying parallelism and implementing parallel algorithms using MPI constructs.
Web Pointers

- MPI standard: [http://www.mpi-forum.org/docs/docs.html](http://www.mpi-forum.org/docs/docs.html)

- MPI implementations:
  - MPICH: [http://www.mpich.org](http://www.mpich.org)
  - MVAPICH: [http://mvapich.cse.ohio-state.edu/](http://mvapich.cse.ohio-state.edu/)
  - Open MPI: [http://www.open-mpi.org/](http://www.open-mpi.org/)
  - IBM MPI, Cray MPI, HP MPI, TH MPI, ...

- Several MPI tutorials can be found on the web
Tutorial Books on MPI

**Using MPI**
Portable Parallel Programming with the Message-Passing Interface
third edition

**Using Advanced MPI**
Modern Features of the Message-Passing Interface

William Gropp
Torsten Hoefler
Rajeev Thakur
Ewing Lusk
Book on Parallel Programming Models

Edited by Pavan Balaji

- **MPI**: W. Gropp and R. Thakur
- **GASNet**: P. Hargrove
- **OpenSHMEM**: J. Kuehn and S. Poole
- **UPC**: K. Yelick and Y. Zheng
- **Global Arrays**: S. Krishnamoorthy, J. Daily, A. Vishnu, and B. Palmer
- **Chapel**: B. Chamberlain
- **Charm++**: L. Kale, N. Jain, and J. Lifflander
- **ADLB**: E. Lusk, R. Butler, and S. Pieper
- **Scioto**: J. Dinan
- **SWIFT**: T. Armstrong, J. M. Wozniak, M. Wilde, and I. Foster
- **CnC**: K. Knobe, M. Burke, and F. Schlimbach
- **OpenMP**: B. Chapman, D. Eachempati, and S. Chandrasekaran
- **Cilk Plus**: A. Robison and C. Leiserson
- **Intel TBB**: A. Kukanov
- **CUDA**: W. Hwu and D. Kirk
- **OpenCL**: T. Mattson
Approach in this Tutorial

- Example driven
  - A few running examples used throughout the tutorial
  - Other smaller examples used to illustrate specific features
Costs of Unintended Synchronization
Unexpected Hot Spots

- Even simple operations can give surprising performance behavior
- Examples arise even in common grid exchange patterns
- Message passing illustrates problems present even in shared memory
  - Blocking operations may cause unavoidable stalls
Mesh Exchange

- Exchange data on a mesh
Sample Code

- Do i=1,n_neighbors
  - Call MPI_Send(edge(1,i), len, MPI_REAL, &nbr(i), tag, comm, ierr)
Enddo

Do i=1,n_neighbors
  - Call MPI_Recv(edge(1,i), len, MPI_REAL, &nbr(i), tag, comm, status, ierr)
Enddo
Deadlocks!

- All of the sends may block, waiting for a matching receive (will for large enough messages)
- The variation of
  
  ```
  if (has down nbr) then
      Call MPI_Send( ... down ... )
  endif
  
  if (has up nbr) then
      Call MPI_Recv( ... up ... )
  endif
  ...
  ```

  sequentializes (all except the bottom process blocks)
## Sequentialization

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**20**
Fix 1: Use Irecv

- Do i=1, n_neighbors
  
  Call MPI_Irecv(inedge(1,i), len, MPI_REAL, nbr(i), tag, &comm, requests(i), ierr)

Enddo

- Do i=1, n_neighbors
  
  Call MPI_Send(edge(1,i), len, MPI_REAL, nbr(i), tag, &comm, ierr)

Enddo

- Call MPI_Waitall(n_neighbors, requests, statuses, ierr)

- Does not perform well in practice. Why?
Understanding the Behavior: Timing Model

- Sends interleave
- Sends block (data larger than buffering will allow)
- Sends control timing
- Receives do not interfere with Sends
- Exchange can be done in 4 steps (down, right, up, left)
Mesh Exchange - Step 1

- Exchange data on a mesh
Mesh Exchange - Step 2

- Exchange data on a mesh
Mesh Exchange - Step 3

- Exchange data on a mesh
Mesh Exchange - Step 4

- Exchange data on a mesh
Mesh Exchange - Step 5

- Exchange data on a mesh
Mesh Exchange - Step 6

- Exchange data on a mesh
Timeline

- Note that process 1 finishes last, as predicted
Distribution of Sends

'SEND' state length distribution

(in seconds)

58 states of 56 (70%)
Why Six Steps?

- Ordering of Sends introduces delays when there is contention at the receiver
- Takes roughly twice as long as it should
- Bandwidth is being wasted
- Same thing would happen if using memcpy and shared memory
Fix 2: Use Isend and Irecv

- Do i=1, n_neighbors
  
  Call MPI_Irecv(inedge(1,i), len, MPI_REAL, nbr(i), tag, &comm, requests(i), ierr)

  Enddo

- Do i=1, n_neighbors
  
  Call MPI_Isend(edge(1,i), len, MPI_REAL, nbr(i), tag, &comm, requests(n_neighbors+i), ierr)

  Enddo

- Call MPI_Waitall(2*n_neighbors, requests, statuses, ierr)
Mesh Exchange - Steps 1-4

- Four interleaved steps
Note processes 5 and 6 are the only interior processes; these perform more communication than the other processes.
Lesson: Defer Synchronization

- Send-receive accomplishes two things:
  - Data transfer
  - Synchronization

- In many cases, there is more synchronization than required

- Consider the use of nonblocking operations and MPI_Waitall to defer synchronization
  - Effectiveness depends on how data is moved by the MPI implementation
  - E.g., If large messages are moved by blocking RMA operations “under the covers,” the implementation can’t adapt to contention at the target processes, and you may see no benefit.
  - This is more likely with larger messages
Collectives: Blocking and Nonblocking
Introduction to Collective Operations in MPI

- Collective operations are called by all processes in a communicator.
- `MPI_BCAST` distributes data from one process (the root) to all others in a communicator.
- `MPI_REDUCE` combines data from all processes in the communicator and returns it to one process.
- In many numerical algorithms, `SEND/RECV` can be replaced by `BCAST/REDUCE`, improving both simplicity and efficiency.
MPI Collective Communication

- Communication and computation is coordinated among a group of processes in a communicator
- Tags are not used; different communicators deliver similar functionality
- Non-blocking collective operations in MPI-3
- Three classes of operations: synchronization, data movement, collective computation
Synchronization

- **MPI_BARRIER**(comm)
  - Blocks until all processes in the group of the communicator **comm** call it
  - A process cannot get out of the barrier until all other processes have reached barrier
Collective Data Movement

Broadcast

Gather

Scatter
More Collective Data Movement

**Allgather**

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**Alltoall**

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Collective Computation

Reduce

Scan

f(ABCD)
f(A)
f(AB)
f(ABC)
f(ABCD)
MPI Collective Routines

- Many Routines: \texttt{MPI\_ALLGATHER}, \texttt{MPI\_ALLGATHERV}, \texttt{MPI\_ALLREDUCE}, \texttt{MPI\_ALLTOALL}, \texttt{MPI\_ALLTOALLV}, \texttt{MPI\_BCAST}, \texttt{MPI\_GATHER}, \texttt{MPI\_GATHERV}, \texttt{MPI\_REDUCE}, \texttt{MPI\_REDUCESCATTER}, \texttt{MPI\_SCAN}, \texttt{MPI\_SCATTER}, \texttt{MPI\_SCATTERV}
- "All" versions deliver results to all participating processes
- "V" versions (stands for vector) allow the chunks to have different sizes
- \texttt{MPI\_ALLREDUCE}, \texttt{MPI\_REDUCE}, \texttt{MPI\_REDUCESCATTER}, and \texttt{MPI\_SCAN} take both built-in and user-defined combiner functions
MPI Built-in Collective Computation Operations

- **MPI_MAX**: Maximum
- **MPI_MIN**: Minimum
- **MPI_PROD**: Product
- **MPI_SUM**: Sum
- **MPI_LAND**: Logical and
- **MPI_LOR**: Logical or
- **MPI_LXOR**: Logical exclusive or
- **MPI_BAND**: Bitwise and
- **MPI_BOR**: Bitwise or
- **MPI_BXOR**: Bitwise exclusive or
- **MPI_MAXLOC**: Maximum and location
- **MPI_MINLOC**: Minimum and location
Defining your own Collective Operations

- Create your own collective computations with:

  ```c
  MPI_OP_CREATE(user_fn, commutes, &op);
  MPI_OP_FREE(&op);
  user_fn(invec, inoutvec, len, datatype);
  ```

- The user function should perform:

  ```c
  for i from 0 to len-1
      inoutvec[i] = invec[i] op inoutvec[i];
  ```

- The user function can be non-commutative, but must be associative
Example: Calculating Pi (1/3)

- Calculating the value of “pi” via numerical integration
  - Divide interval up into subintervals
  - Assign subintervals to processes
  - Each process calculates partial sum
  - Add all the partial sums together to get pi

1. Width of each segment (w) will be 1/n
2. Distance (d(i)) of segment “i” from the origin will be “i * w”
3. Height of segment “i” will be sqrt(1 – [d(i)]^2)
```c
#include <mpi.h>
#include <math.h>
int main(int argc, char *argv[]) {
    [...snip...]
    /* Tell all processes, the number of segments you want */
    MPI_Bcast(&n, 1, MPI_INT, 0, MPI_COMM_WORLD);
    w   = 1.0 / (double) n;
    mypi = 0.0;
    for (i = rank + 1; i <= n; i += size)
        mypi += w * sqrt(1 - ((double) i / n) * ((double) i / n));
    MPI_Reduce(&mypi, &pi, 1, MPI_DOUBLE, MPI_SUM, 0, MPI_COMM_WORLD);
    if (rank == 0)
        printf("pi is approximately %.16f, Error is %.16f\n", 4 * pi, fabs((4 * pi) - PI25DT));
    [...snip...]
}
```

Example: Calculating Pi (2/3)
Example: Calculating Pi (3/3)

- `blocking_coll/cpi.c`
- Calculating the approximate value of PI in parallel
Nonblocking Collective Communication

- Nonblocking (send/recv) communication
  - Deadlock avoidance
  - Overlapping communication/computation

- Collective communication
  - Collection of pre-defined optimized routines

- Nonblocking collective communication
  - Combines both techniques
  - System noise/imbalance resiliency
  - Semantic advantages
Nonblocking Collective Communication

- Nonblocking variants of all collectives
  - `MPI_Ibcast(<bcast args>, MPI_Request *req);`

- Semantics
  - Function returns no matter what
  - No guaranteed progress (quality of implementation)
  - Usual completion calls (wait, test) + mixing
  - Out-of-order completion

- Restrictions
  - Send and vector buffers may not be updated during operation (like other nonblocking operations)
  - No tags, in-order matching (like other collective operations)
  - `MPI_Cancel` not supported
  - No matching with blocking collectives
Nonblocking Collective Communication

- Semantic advantages
  - Enable asynchronous progression (and manual)
    - Software pipelining
  - Decouple data transfer and synchronization
    - Noise resiliency!
  - Allow overlapping communicators
    - See also neighborhood collectives
  - Multiple outstanding operations at any time
    - Enables pipelining window
A Nonblocking Barrier?

- **Semantics:**
  - `MPI_Ibarrier()` – calling process entered the barrier, **no** synchronization happens
  - Synchronization **may** happen asynchronously
  - `MPI_Test/Wait()` – synchronization happens **if** necessary

- **Uses:**
  - Overlap barrier latency (small benefit)
  - Use the split semantics! Processes **notify** noncollectively but **synchronize** collectively!
Section Summary

- Collectives are a very powerful feature in MPI
- Optimized heavily in most MPI implementations
  - Algorithmic optimizations (e.g., tree-based communication)
  - Hardware optimizations (e.g., network or switch-based collectives)
- Matches the communication pattern of many applications
- Nonblocking collectives combine the semantics of nonblocking point-to-point and blocking collectives
- Natural extension to blocking collectives for event-driven programming
- Hardware implementations already exist for most (but not all) nonblocking collectives
Running Example: Stencil
Running Example: Regular Mesh Algorithms

- Many scientific applications involve the solution of partial differential equations (PDEs)
- Many algorithms for approximating the solution of PDEs rely on forming a set of difference equations
  - Finite difference, finite elements, finite volume
- The exact form of the differential equations depends on the particular method
  - From the point of view of parallel programming for these algorithms, the operations are the same
- Five-point stencil is a popular approximation solution
The Global Data Structure

- Each circle is a mesh point
- Difference equation evaluated at each point involves the four neighbors
- The red “plus” is called the method’s stencil
- Good numerical algorithms form a matrix equation $Au=f$; solving this requires computing $Bv$, where $B$ is a matrix derived from $A$. These evaluations involve computations with the neighbors on the mesh.
The Global Data Structure

- Each circle is a mesh point
- Difference equation evaluated at each point involves the four neighbors
- The red “plus” is called the method’s stencil
- Good numerical algorithms form a matrix equation $Au=f$; solving this requires computing $Bv$, where $B$ is a matrix derived from $A$. These evaluations involve computations with the neighbors on the mesh.
- Decompose mesh into equal sized (work) pieces
Domain Decomposition

Parameters for domain decomposition:
N = Size of the edge of the global problem domain (assuming square)
PX, PY = Number of processes in X and Y dimension
N % PX == 0, N % PY == 0

Where am I? (Global offset)
Who (which ranks) are my neighbors?
Use MPI_PROC_NULL for boundary
Necessary Data Transfers
The Local Data Structure

- Each process has its local “patch” of the global array
  - “bx” and “by” are the sizes of the local array
  - Always allocate a halo around the patch
  - Array allocated of size (bx+2)x(by+2)

Check the alloc_bufs function to see how buffers are allocated
Necessary Data Transfers

- Provide access to remote data through a halo exchange  (5 point stencil)

Check the `update_grid` function to see how it is done
MPI Examples on Cooley

- `/lus/theta-fs0/projects/ATPESC2020/mpi`
- Copy to your own project directory
- Submit job using “ATPESC2020” project, and “training” queue to use the reservation
Example: Stencil with Nonblocking Send/recv

- `nonblocking_p2p/stencil.c`
- Simple stencil code using nonblocking point-to-point operations

```
# make
# qsub -A ATPESC2020 -q training -n <nproc> -t 10 ./job.sh

# mpirun -n <nproc> ./stencil <domain size> <heat source value> <iterations> <px> <py>
```
Derived Datatypes
Introduction to Datatypes in MPI

- Datatypes allow to (de)serialize **arbitrary** data layouts into a message stream
  - Networks provide serial channels
  - Same for block devices and I/O

- Several constructors allow arbitrary layouts
  - Recursive specification possible
  - *Declarative* specification of data-layout
    - “what” and not “how”, leaves optimization to implementation (*many unexplored* possibilities!)
  - Choosing the right constructors is not always simple
Simple/Predefined Datatypes

- Equivalents exist for all C, C++ and Fortran native datatypes
  - C int → MPI_INT
  - C float → MPI_FLOAT
  - C double → MPI_DOUBLE
  - C uint32_t → MPI_UINT32_T
  - Fortran integer → MPI_INTEGER

- For more complex or user-created datatypes, MPI provides routines to represent them as well
  - Contiguous
  - Vector/Hvector
  - Indexed/Indexed_block/Hindexed/Hindexed_block
  - Struct
  - Some convenience types (e.g., subarray)
Derived Datatype Example
MPI_Type_contiguous

- Contiguous array of oldtype
- Should not be used as last type (can be replaced by count)
**MPI_Type_vector**

- Specify strided blocks of data of oldtype
- Very useful for Cartesian arrays

```c
MPI_Type_vector(int count, int blocklen, int stride, MPI_Datatype oldtype, MPI_Datatype *newtype)
```
Commit, Free, and Dup

- Types must be committed before use
  - Only the ones that are used!
  - MPI_Type_commit may perform heavy optimizations (and will hopefully)
- MPI_Type_free
  - Free MPI resources of datatypes
  - Does not affect types built from it
- MPI_Type_dup
  - Duplicates a type
  - Library abstraction (composability)
MPI_Type_create_hvector

- Create byte strided vectors
- Useful for composition, e.g., vector of structs
MPI_Type_create_indexed_block

- Pulling irregular subsets of data from a single array
  - dynamic codes with index lists, expensive though!
  - blen=2
  - displs={0,5,8,13,18}
MPI_Type_indexed

- Like indexed_block, but can have different block lengths
  - blen={1,1,2,1,2,1}
  - displs={0,3,5,9,13,17}

```c
MPI_Type_indexed(int count, int* array_of_blocklens, int *array_of_displacements,
                 MPI_Datatype oldtype, MPI_Datatype *newtype)
```
MPI_Type_create_struct

- Most general constructor, allows different types and arbitrary arrays (also most costly)
MPI_Type_create_subarray

- Convenience function for creating datatypes for array segments
- Specify subarray of n-dimensional array (sizes) by start (starts) and size (subsize)

```
MPI_Type_create_subarray(int ndims, int* array_of_sizes, int *array_of_subsizes,
                          int *array_of_starts, int order, MPI_Datatype oldtype,
                          MPI_Datatype *newtype)
```
Section Summary

- Derived datatypes are a sophisticated mechanism to describe ANY layout in memory
  - Hierarchical construction of derived datatypes allows them to be just as complex as the data layout is
  - More complex layouts require more complex datatype constructions

- Current state of MPI implementations might be a bit lagging in performance, but it is improving
  - Increasing amount of hardware support to process derived datatypes on the network hardware
  - If the performance is lagging when you try it out, complain to the MPI implementer, don’t just stop using it!
Exercise: Stencil with Derived Datatypes (1/2)

- In the basic version of the stencil code
  - Used nonblocking communication 👍
  - Used manual packing/unpacking of data 👎

- Let’s try to use derived datatypes
  - Specify the locations of the data instead of manually packing/unpacking

What datatype do we need here?

What datatype do we need here?
Exercise: Stencil with Derived Datatypes (2/2)

- Nonblocking sends and receives
- Data location specified by MPI datatypes
- Manual packing of data no longer required
- Start from nonblocking_p2p/stencil.c
- Solution in derived_datatype/stencil.c
MPI One-sided Communication
One-sided Communication

- The basic idea of one-sided communication models is to decouple data movement with process synchronization
  - Should be able to move data without requiring that the remote process synchronize
  - Each process exposes a part of its memory to other processes
  - Other processes can directly read from or write to this memory
Two-sided Communication Example
One-sided Communication Example
Comparing One-sided and Two-sided Programming

Even the sending process is delayed

Delay in process 1 does not affect process 0
What we need to know in MPI RMA

- How to create remote accessible memory?
- Reading, Writing and Updating remote memory
- Data Synchronization
- Memory Model
Creating Public Memory

- Any memory used by a process is, by default, only locally accessible
  - `X = malloc(100);`

- Once the memory is allocated, the user has to make an explicit MPI call to declare a memory region as remotely accessible
  - MPI terminology for remotely accessible memory is a "window"
  - A group of processes collectively create a "window"

- Once a memory region is declared as remotely accessible, all processes in the window can read/write data to this memory without explicitly synchronizing with the target process
Window creation models

Four models exist

- **MPI_WIN_ALLOCATE**
  - You want to create a buffer and directly make it remotely accessible

- **MPI_WIN_CREATE**
  - You already have an allocated buffer that you would like to make remotely accessible

- **MPI_WIN_CREATE_DYNAMIC**
  - You don’t have a buffer yet, but will have one in the future
  - You may want to dynamically add/remove buffers to/from the window

- **MPI_WIN_ALLOCATE_SHARED**
  - You want multiple processes on the same node share a buffer
**MPI_WIN_ALLOCATE**

Create a remotely accessible memory region in an RMA window

- Only data exposed in a window can be accessed with RMA ops.

**Arguments:**

- `size` - size of local data in bytes (nonnegative integer)
- `disp_unit` - local unit size for displacements, in bytes (positive integer)
- `info` - info argument (handle)
- `comm` - communicator (handle)
- `baseptr` - pointer to exposed local data
- `win` - window (handle)

```c
MPI_Win_allocate(MPI_Aint size, int disp_unit, MPI_Info info, MPI_Comm comm,
                void *baseptr, MPI_Win *win)
```
int main(int argc, char ** argv)
{
    int *a;
    MPI_Win win;

    MPI_Init(&argc, &argv);

    /* collectively create remote accessible memory in a window */
    MPI_Win_allocate(1000*sizeof(int), sizeof(int), MPI_INFO_NULL, MPI_COMM_WORLD, &a, &win);

    /* Array ‘a’ is now accessible from all processes in
    * MPI_COMM_WORLD */

    MPI_Win_free(&win);

    MPI_Finalize(); return 0;
}
MPI_WIN_CREATE

Expose a region of memory in an RMA window
  - Only data exposed in a window can be accessed with RMA ops.

Arguments:
  - base    - pointer to local data to expose
  - size    - size of local data in bytes (nonnegative integer)
  - disp_unit - local unit size for displacements, in bytes (positive integer)
  - info    - info argument (handle)
  - comm    - communicator (handle)
  - win     - window (handle)

MPI_Win_create(void *base, MPI_Aint size, int disp_unit, MPI_Info info, MPI_Comm comm, MPI_Win *win)
Example with MPI_WIN_CREATE

```c
int main(int argc, char ** argv)
{
    int *a; MPI_Win win;

    MPI_Init(&argc, &argv);

    /* create private memory */
    a = (int *) malloc(1000*sizeof(int));
    /* use private memory like you normally would */
    for (int i = 0; i < 1000; i++) a[i] = i + 1;

    /* collectively declare memory as remotely accessible */
    MPI_Win_create(a, 1000*sizeof(int), sizeof(int), MPI_INFO_NULL, MPI_COMM_WORLD, &win);

    /* Array 'a' is now accessibly by all processes in
    * MPI_COMM_WORLD */

    MPI_Win_free(&win);
    free(a);
    MPI_Finalize(); return 0;
}
```
**MPI_WIN_CREATE_DYNAMIC**

- Create an RMA window, to which data can later be attached
  - Only data exposed in a window can be accessed with RMA ops

- Initially "empty"
  - Application can dynamically attach/detach memory to this window by calling
    \[\text{MPI_Win_attach/detach}\]
  - Application can access data on this window only after a memory region has been attached

- Window origin is **MPI_BOTTOM**
  - Displacements are segment addresses relative to **MPI_BOTTOM**
  - Must tell others the displacement after calling attach
Example with MPI_WIN_CREATE_DYNAMIC

```c
int main(int argc, char ** argv)
{
    int *a;    MPI_Win win;

    MPI_Init(&argc, &argv);
    MPI_Win_create_dynamic(MPI_INFO_NULL, MPI_COMM_WORLD, &win);

    /* create private memory */
    a = (int *) malloc(1000 * sizeof(int));
    /* use private memory like you normally would */
    for (int i = 0; i < 1000; i++) a[i] = i + 1;

    /* locally declare memory as remotely accessible */
    MPI_Win_attach(win, a, 1000*sizeof(int));

    /* Array `a` is now accessible from all processes */

    /* undeclare remotely accessible memory */
    MPI_Win_detach(win, a); free(a);
    MPI_Win_free(&win);

    MPI_Finalize(); return 0;
}
```
Data movement

- MPI provides ability to read, write and atomically modify data in remotely accessible memory regions
  - MPI_PUT
  - MPI_GET
  - MPI_ACCUMULATE (atomic)
  - MPI_GET_ACCUMULATE (atomic)
  - MPI_COMPARE_AND_SWAP (atomic)
  - MPI_FETCH_AND_OP (atomic)
Data movement: \textit{Put}

- Move data \textbf{from} origin, \textbf{to} target
- Separate data description triples for \textit{origin} and \textit{target}

\begin{verbatim}
MPI_Put(const void *origin_addr, int origin_count, MPI_Datatype origin_dtype,
        int target_rank, MPI_Aint target_disp, int target_count,
        MPI_Datatype target_dtype, MPI_Win win)
\end{verbatim}
Data movement: *Get*

- Move data to *origin*, from *target*
- Separate data description triples for *origin* and *target*

```c
MPI_Get(void *origin_addr, int origin_count, MPI_Datatype origin_dtype,
        int target_rank, MPI_Aint target_disp, int target_count,
        MPI_Datatype target_dtype, MPI_Win win)
```
Atomic Data Aggregation: *Accumulate*

- Atomic update operation, similar to a put
  - Reduces origin and target data into target buffer using op argument as combiner
  - \( \text{Op} = \text{MPI\_SUM}, \text{MPI\_PROD}, \text{MPI\_OR}, \text{MPI\_REPLACE}, \text{MPI\_NO\_OP}, \ldots \)
  - Predefined ops only, no user-defined operations
- Different data layouts between target/origin OK
  - Basic type elements must match
- \( \text{Op} = \text{MPI\_REPLACE} \)
  - Implements \( f(a,b) = b \)
  - Atomic PUT

**MPI\_Accumulate**

\[
\text{MPI\_Accumulate}(\text{const void *origin\_addr}, \text{int origin\_count}, \text{MPI\_Datatype origin\_dtype}, \\
\text{int target\_rank}, \text{MPI\_Aint target\_disp}, \text{int target\_count}, \\
\text{MPI\_Datatype target\_dtype}, \text{MPI\_Op op}, \text{MPI\_Win win})
\]
Atomic Data Aggregation: *Get Accumulate*

**Function declaration:**

```c
MPI_Get_accumulate(const void *origin_addr, int origin_count, MPI_Datatype origin_dtype,
                    void *result_addr, int result_count, MPI_Datatype result_dtype,
                    int target_rank, MPI_Aint target_disp, int target_count,
                    MPI_Datatype target_dtype, MPI_Op op, MPI_Win win)
```

- Atomic read-modify-write
  - $Op = \text{MPI\_SUM}, \text{MPI\_PROD}, \text{MPI\_OR}, \text{MPI\_REPLACE}, \text{MPI\_NO\_OP}, \ldots$
  - Predefined ops only
- Result stored in target buffer
- Original data stored in result buf
- Different data layouts between target/origin OK
  - Basic type elements must match
- Atomic get with **MPI\_NO\_OP**
- Atomic swap with **MPI\_REPLACE**
Atomic Data Aggregation: *FOP and CAS*

- **FOP:** Simpler version of MPI\_Get\_accumulate
  - All buffers share a single predefined datatype
  - No count argument (it’s always 1)
  - Simpler interface allows hardware optimization

- **CAS:** Atomic swap if target value is equal to compare value

```c
MPIFetch_and_op(const void *origin_addr, void *result_addr, MPI_Datatype dtype,
                int target_rank, MPI_Aint target_disp, MPI_Op op, MPI_Win win)

MPICompare_and_swap(const void *origin_addr, const void *compare_addr,
                    void *result_addr, MPI_Datatype dtype, int target_rank, 
                    MPI_Aint target_disp, MPI_Win win)
```
Ordering of Operations in MPI RMA

- No guaranteed ordering for Put/Get operations
- Result of concurrent Puts to the same location undefined
- Result of Get concurrent Put/Accumulate undefined
  - Can be garbage in both cases
- Result of concurrent accumulate operations to the same location are defined according to the order in which the occurred
  - Atomic put: Accumulate with op = MPI_REPLACE
  - Atomic get: Get_accumulate with op = MPI_NO_OP
- Accumulate operations from a given process are ordered by default
  - User can tell the MPI implementation that (s)he does not require ordering as optimization hint
  - You can ask for only the needed orderings: RAW (read-after-write), WAR, RAR, or WAW
Examples with operation ordering

1. Concurrent Puts: **undefined**

2. Concurrent Get and Put/Accumulates: **undefined**

3. Concurrent Accumulate operations to the same location: **ordering is guaranteed**
RMA Synchronization Models

- RMA data access model
  - When is a process allowed to read/write remotely accessible memory?
  - When is data written by process X available for process Y to read?
  - RMA synchronization models define these semantics

- Three synchronization models provided by MPI:
  - Fence (active target)
  - Post-start-complete-wait (generalized active target)
  - Lock/Unlock (passive target)

- Data accesses occur within “epochs”
  - *Access epochs*: contain a set of operations issued by an origin process
  - *Exposure epochs*: enable remote processes to update a target’s window
  - Epochs define ordering and completion semantics
  - Synchronization models provide mechanisms for establishing epochs
    - E.g., starting, ending, and synchronizing epochs
Fence: Active Target Synchronization

- Collective synchronization model
- Starts *and* ends access and exposure epochs on all processes in the window
- All processes in group of “win” do an `MPI_WIN_FENCE` to open an epoch
- Everyone can issue `PUT/GET` operations to read/write data
- Everyone does an `MPI_WIN_FENCE` to close the epoch
- All operations complete at the second fence synchronization

```c
MPI_Win_fence(int assert, MPI_Win win)
```
Exercise 1: Stencil with RMA Fence (1/2)

- Origin buffers
- Target buffers
- RMA window
Exercise 1: Stencil with RMA Fence (2/2)

- In the derived datatype version of the stencil code
  - Used nonblocking communication
  - Used derived datatypes
- Let’s try to use RMA fence
  - Move data with PUT instead of send/recv
- *Start from derived_datatype/stencil.c*
- *Solution available in rma/stencil_fence_put.c*
Exercise 2: Stencil with RMA Fence (GET model)

- In the derived datatype version of the stencil code
  - Used nonblocking communication
  - Used derived datatypes

- Let’s try to use RMA fence
  - Move data with GET instead of send/recv

- Start from rma/stencil_fence_put.c

- Solution available in rma/stencil_fence_get.c
PSCW: Generalized Active Target Synchronization

- Like FENCE, but origin and target specify who they communicate with

- Target: Exposure epoch
  - Opened with `MPI_Win_post`
  - Closed by `MPI_Win_wait`

- Origin: Access epoch
  - Opened by `MPI_Win_start`
  - Closed by `MPI_Win_complete`

- All synchronization operations may block, to enforce P-S/C-W ordering
  - Processes can be both origins and targets

```c
MPI_Win_post/start(MPI_Group grp, int assert, MPI_Win win)
MPI_Win_complete/wait(MPI_Win win)
```
Exercise 3: Stencil with RMA PSCW (PUT model)

- In the fence version of the stencil code
  - Unnecessary synchronization between all processes

- Let’s try to use RMA PSCW
  - Synchronize with PSCW instead of Fence

- Start from rma/stencil_fence_put.c

- Solution available in rma/stencil_pscw_put.c
Lock/Unlock: Passive Target Synchronization

- Passive mode: One-sided, *asynchronous* communication
  - Target does *not* participate in communication operation
- Shared memory-like model
Passive Target Synchronization

- **Lock/Unlock**: Begin/end passive mode epoch
  - Target process does not make a corresponding MPI call
  - Can initiate multiple passive target epochs to different processes
  - Concurrent epochs to same process not allowed (affects threads)

- **Lock type**
  - **SHARED**: Other processes using shared can access concurrently
  - **EXCLUSIVE**: No other processes can access concurrently

- **Flush**: Remotely complete RMA operations to the target process
  - After completion, data can be read by target process or a different process

- **Flush_local**: Locally complete RMA operations to the target process

```c
MPI_Win_lock(int locktype, int rank, int assert, MPI_Win win)
MPI_Win_unlock(int rank, MPI_Win win)
MPI_Win_flush/flush_local(int rank, MPI_Win win)
```
Advanced Passive Target Synchronization

- **Lock_all**: Shared lock, passive target epoch to all other processes
  - Expected usage is long-lived: `lock_all, put/get, flush, ..., unlock_all`

- **Flush_all** – remotely complete RMA operations to all processes

- **Flush_local_all** – locally complete RMA operations to all processes
MPI RMA Memory Model

- MPI-3 provides two memory models: separate and unified
- Separate Model
  - Logical public and private copies
  - MPI provides software coherence between window copies
  - Extremely portable, to systems that don’t provide hardware coherence
- New Unified Model
  - Single copy of the window
  - System must provide coherence
  - Superset of separate semantics
    - E.g. allows concurrent local/remote access
  - Provides access to full performance potential of hardware
**MPI RMA Memory Model (separate windows)**

- Very portable, compatible with non-coherent memory systems
- Limits concurrent accesses to enable software coherence
MPI RMA Memory Model (unified windows)

- Allows concurrent local/remote accesses
- Concurrent, conflicting operations are allowed (not invalid)
  - Outcome is not defined by MPI (defined by the hardware)
- Can enable better performance by reducing synchronization
### MPI RMA Operation Compatibility (Separate)

<table>
<thead>
<tr>
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<th>Load</th>
<th>Store</th>
<th>Get</th>
<th>Put</th>
<th>Acc</th>
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<tr>
<td>Put</td>
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<td>X</td>
<td>NOVL</td>
<td>NOVL</td>
<td>OVL+NOVL</td>
</tr>
</tbody>
</table>

This matrix shows the compatibility of MPI-RMA operations when two or more processes access a window at the same target concurrently.

- **OVL** – Overlapping operations permitted
- **NOVL** – Nonoverlapping operations permitted
- **X** – Combining these operations is OK, but data might be garbage
### MPI RMA Operation Compatibility (Unified)

<table>
<thead>
<tr>
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<th>Load</th>
<th>Store</th>
<th>Get</th>
<th>Put</th>
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This matrix shows the compatibility of MPI-RMA operations when two or more processes access a window at the same target concurrently.

**OVL** – Overlapping operations permitted  
**NOVL** – Nonoverlapping operations permitted
Synchronizing Local and RMA Access (1/2)

- RMA operations access the public copy of window
- Local load/store update the private copy
  - Including using as MPI send/receive buffers
- Ensure memory synchronization for portability
- Implicit memory synchronization (i.e., memory barrier) in RMA synchronization calls
  - **Fence**: Synchronize private and public copies of local window
Synchronizing Local and RMA Access (2/2)

- **PSCW active target epoch**
  - **Post**: Updates in private copy becomes visible in public copy
  - **Wait**: Updates in public copy becomes visible in private copy

- **Passive target epoch**
  - **Lock/Lock_all**: Updates in public copy becomes visible in private
  - **Unlock/Unlock_all**: Updates in private copy becomes visible in public
Window synchronization: MPI_WIN_SYNC

- Synchronizes the public and private copies of local window in passive target epoch

```
MPI_Win_sync(MPI_Win win)
```

---

**Diagram:**

- Lock(shared, P1)
- ... (Other operations)
- Barrier
- GET(x, P1)
- PUT(y=1, P1)
- Flush(P1)
- Unlock(P1)
- Barrier

---

- Lock(shared, P1)
- store x = 1
- Win_sync
- Barrier
- Public Copy
- Private Copy
- Win_sync
- Barrier
- Public Copy
- Private Copy
- Barrier
- load y
- Unlock(P1)
Exercise 4: Stencil with RMA Lock_all/Unlock_all (PUT model)

- In the fence and PSCW versions of the stencil code, RMA synchronization involves the target processes.

- Let’s try to use RMA Lock_all/Flush_all/Unlock_all
  - Only the origin processes call RMA synchronization.
  - Still need **Barrier** for process synchronization (e.g., ensure neighbors have completed data update to my local window).
  - Need **Win_sync** for memory synchronization.

- **Start from rma/stencil_fence_put.c**

- **Solution available in rma/stencil_lock_put.c**
Example: Block Sparse Matrix Multiplication
NWChem [1]

- High performance computational chemistry application suite
- Quantum level simulation of molecular systems
  - Very expensive in computation and data movement, so is used for small systems
  - Larger systems use molecular level simulations
- Composed of many simulation capabilities
  - Molecular Electronic Structure
  - Quantum Mechanics/Molecular Mechanics
  - Pseudo potential Plane-Wave Electronic Structure
  - Molecular Dynamics
- Very large code base
  - 4M LOC; Total investment of ~200M $ to date

NWChem Communication Runtime

Global Arrays \[^{[2]}\]

ARMCI: Communication interface for RMA \[^{[3]}\]

ARMCI native ports
- IB
- DMMAP
- ...\n
ARMCI-MPI

MPI RMA

Abstractions for distributed arrays

Get

Put

Global Address Space

Physically distributed to different processes

Hidden from user

Irregularly access large amount of remote memory regions

Block Sparse Matrix Multiplication (BSPMM)

- Computing block sparse matrix multiplication: $C = \alpha A \times B + \beta C$

Mock figure showing 2D DGEMM with block-sparse computations. In reality, NWChem uses 6D tensors.
The Global Data Structure

- Applications operate on large data sets that easily exceed the capacity of a single node
  - Resource sharing across nodes becomes necessary
  - "Allocate" matrices in the global address space that is physically distributed onto different nodes
- In the tutorial, the first process entirely allocates all three matrices for simplicity
The Parallel Approach

- Divide to independent subblocks and distribute over processes
- Compute DGEMM of subblocks locally
- For each $c_{ij}$, sum up the results of corresponding subblock multiplication

![Diagram showing parallel processing](image)

A-based parallelism
Set $\alpha=1$, $\beta=0$ for simplicity, compute $C = AB$
Example: BSPMM with full matrices

- `blocking_p2p/bspmm_simple.c`
- Simple bspmm code using blocking point-to-point operations
  - Rank 0 (master) initializes all matrices and sends the entire A and B matrices to other processes (workers)
  - Each worker computes different blocks and sends the local matrix C to master
  - Master sums up the received results

```
A
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```

worker 0
- Compute C0

worker 1
- Compute C1

master
- Sum C=C0+C1
Example: BSPMM with RMA

- *rma/bspmm.c*
- Only synchronization from origin processes (workers), no synchronization from target processes (implicit master)
- Replace send/receive with RMA Get and Accumulate

```
get a, b
compute c=a*b
accumulate c
```

```
get a, b
compute c=a*b
accumulate c
```
Exercise 5: BSPMM using global counter (atomics)

- In the basic RMA version of BSPMM, we statically assigned the ownership of blocks for each process
  - Load imbalance: e.g., one process may get more zero-blocks than others
- Let us implement a dynamic task secluding
  - Each process dynamically “queries” the next available block computation once finished the previous one (A-based parallelism)
  - Use atomic `Fetch_and_op(SUM)` with a “global counter”

- Start from `rma/bspmm.c`
- Solution available in `rma/bspmm_counter.c`

```
rank 0
FOP(counter) -> 0
compute a11*b1j

FOP(counter) -> 2
compute a13*b3j
...

rank 1
FOP(counter) -> 1
compute a12*b2j
FOP(counter) -> 3
Skip (a21)
FOP(counter) -> 4
compute a22*b2j
...
```

```
A

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</table>
```

FOP(counter) -&gt; 0
compute a11*b1j
Hardware-Offloaded Communication

- Offloading data transfer to hardware is ideal for performance
  - Two-sided (e.g., SEND/RECEIVE):
    - Require **complex message matching** (rank + tag + comm), especially for wildcard receives (MPI_ANY_TAG|ANY_SOURCE)
    - Supported HW: Mellanox ConnectX-5 (support HW tag matching)
  - One-sided (e.g., PUT/GET/ACCUMUALTE):
    - **No matching** requirement, easier for hardware offloading
    - Natively supported on various RDMA networks such as Mellanox InfiniBand, Cray Aries, and Fujitsu Tofu

Hardware-offloaded data transfer can be fully overlapped with computation
Asynchronous Execution of MPI RMA

- Asynchronous execution of RMA depends on the MPI implementation, which in turn depends on what the network hardware provides.
- Most common situation on current network hardware:
  - Some operations are natively supported in hardware (e.g., contiguous PUT/GET)
  - Other operations need to be **emulated in software**

Software implementation of one-sided operations means that **the target process has to make an MPI call to make progress**.
Possible Solution 1: Thread-based Progress (1/2)

- Every MPI process creates a **dedicated helper thread** at MPI_Init
  - Supported by most MPI implementations, but unlikely to be default
  - Might need to turn on some environment variable (check the documentation)
- The thread polls MPI progress for the process while the process is computing
- Dedicates some number of computing cores per process
- Multithreading safety overhead (i.e., MPI internal lock contention between threads, memory barriers)
Possible Solution 1: Thread-based Progress (2/2)

- Available in many mainstream MPI implementations
- Core binding is important! See vendor documentation

**MPICH:**

```
% export MPIR_CVAR_ASYNC_PROGRESS=1
```

**Intel MPI:**

```
% export I_MPI_ASYNC_PROGRESS=1
```

**Cray MPI:**

```
% export MPICH_NEMESIS_ASYNC_PROGRESS=1
% export MPICH_MAX_THREAD_SAFETY=multiple
```
Possible Solution 2: Interrupt-based Progress

- Utilize **hardware interrupts** to awaken a kernel thread when new message arrives
- Examples: Cray MPI DMAPP mode (*deprecated from v7.6.0*), IBM MPI on Blue Gene/P
- Overhead of frequent interrupts, need special hardware support
  - Not a common model for most current networks
Possible Solution 3: Process-based Progress (1/4)

- Casper
  - Dedicating **arbitrary number of cores** (usually 1-4 per multicore node) to “**ghost processes**”
  - **Portable PMPI profiling interface based** design allows integration with any MPI-3 implementations *
  - Transparently replace MPI_COMM_WORLD by COMM_USER_WORLD
  - **Shared memory mapping** between local user and ghost processes
  - Redirect RMA operations to ghost process, thus ghost process ensures communication progress
  - Casper can redirect operations only for **MPI_WIN_ALLOCATE** windows

* MPI-3 **MPI_Win_allocate_shared** function is used to enable shared memory mapping.
Possible Solution 3: Process-based Progress (2/4)

- How to use Casper?
  1. Load Casper between application and MPI library:
     - **Option 1**: dynamic load Casper at execution time
       ```
       % mpicc -o app app.c
       % export LD_PRELOAD=<casper_install_dir>/lib/libcasper.so
       % mpicc -o app app.c -lcasper
       % export CSP_NG=2
       % mpiexec -np 48 -ppn 24 ./app
       /* 48 processes are running on two nodes,  
        * each node has 22 user processes and 2 ghost processes*/
     ```
     - **Option 2**: link with Casper (ensure link order: app.o -lcasper -lmpi)
   2. Set number of ghost processes (dedicated progress core)
Demonstrating communication progress

```
MPI_Win_allocate(sizeof(int), sizeof(int),
    MPI_INFO_NULL, MPI_COMM_WORLD, &a, &win);

if (rank == 0) {
    MPI_Win_lock(MPI_LOCK_SHARED, 1, 0, win);
    for (int x = 0; x < ITER; x++) {
        MPI_Accumulate(..., target = 1, ...);
        MPI_Win_flush(1, win);
    }
    MPI_Win_unlock(1, win);
    MPI_Send(..., dst = 1, ...);
} else {
    MPI_Irecv(..., src = 0, ..., &req);
    for (int x = 0; x < ITER; x++) {
        busy_wait(time);
        MPI_Test(&req, &flag, &stat);
    }
}
MPI_Win_free(&win);
```
Possible Solution 3: Process-based Progress (4/4)

- Performance improvement of NWChem with RMA asynchronous progress

**NWChem DFT task for Carbon 240 with 631G* basis set (Strong Scaling)**

- Original MPI
- Casper (1 Ghost)
- Thread (Dedicate)
- Thread (Oversub with HT)

**NWChem CCSD(T) task for Water 21 with double-zeta basis set (Strong Scaling)**

- Original MPI
- Casper (4 Ghost)
- Thread (Dedicate)
- Thread (Oversub with HT)
Section Summary

- MPI one-sided communication is associated with **windows**
- **Operations** include basic **PUT, GET, and Atomic** operations
- **Synchronization** modes
  - Active-target (similar to two-sided): FENCE, PSCW
  - Passive-target: LOCK-UNLOCK, FLUSH, FLUSH_LOCAL...
- Enable **asynchronous progress** for performance
MPI Hybrid Programming: Threads
Hybrid MPI + X: Most Popular Forms

**MPI + X**

- **Flat MPI**
- **MPI + Threads**
- **MPI + Shared Memory**
- **MPI + ACC**
Why Hybrid MPI+X? Towards Strong Scaling (1/3)

- Strong scaling applications is increasing in importance
  - Hardware limitations: not all resources scale at the same rate as cores (e.g., memory capacity, network resources)
  - Desire to solve the same problem faster on a bigger machine
    - Nek5000, HACC, LAMMPS

- Strong scaling pure MPI applications is getting harder
  - On-node communication is costly compared to load/stores
  - \( O(Px) \) communication patterns (e.g., All-to-all) costly

Evolution of the memory capacity per core in the Top500 list (Peter Kogge. PIM & memory: The need for a revolution in architecture.)
Why Hybrid MPI+X? Towards Strong Scaling (2/3)

- MPI+X benefits ($X=\text{\{threads, MPI shared-memory, etc.\}})$
  - Less memory hungry (MPI runtime consumption, $O(P)$ data structures, etc.)
  - Load/stores to access memory instead of message passing
  - $P$ is reduced by constant $C$ (#cores/process) for $O(Px)$ communication patterns

- Example 1: the Nek5000 team is working at the strong scaling limit

**Nek5000**
Why Hybrid MPI+X? Towards Strong Scaling (3/3)

- Example 2: Quantum Monte Carlo Simulation (QMCPACK)
  - Size of the physical system to simulate is bound by memory capacity [1]
  - Memory space dominated by large interpolation tables (typically several Giga Bytes of storage)
  - Threads are used to share those tables
  - Memory for communication buffers must be kept low to be allow simulation of larger and highly detailed simulations.

MPI + Threads: How To? (1/3)
MPI describes parallelism between \textit{processes} (with separate address spaces)

\textit{Thread} parallelism provides a shared-memory model within a process

OpenMP and Pthreads are common models

- OpenMP provides convenient features for loop-level parallelism. Threads are created and managed by the compiler, based on user directives.
- Pthreads provide more complex and dynamic approaches. Threads are created and managed explicitly by the user.
MPI + Threads: How To? (3/3)

Interoperation or thread levels:

- **MPI_THREAD_SINGLE**
  - No additional threads
- **MPI_THREAD_FUNNELED**
  - Master thread communication only
- **MPI_THREAD_SERIALIZED**
  - Threaded communication serialized
- **MPI_THREAD_MULTIPLE**
  - No restrictions

Interoperability

- **Restriction**
- **Low Thread-Safety Costs**

- **Flexibility**
- **High Thread-Safety Costs**
MPI’s Four Levels of Thread Safety

- MPI defines four levels of thread safety -- these are commitments the application makes to the MPI
- Thread levels are in increasing order
  - If an application works in FUNNELED mode, it can work in SERIALIZED
- MPI defines an alternative to MPI_Init
  - `MPI_Init_thread`(requested, provided): Application specifies level it needs; MPI implementation returns level it supports
MPI_THREAD_SINGLE

- There are no additional user threads in the system
  - E.g., there are no OpenMP parallel regions

```c
int buf[100];
int main(int argc, char ** argv)
{
    MPI_Init(&argc, &argv);
    MPI_Comm_rank(MPI_COMM_WORLD, &rank);
    for (i = 0; i < 100; i++)
        compute(buf[i]);

    /* Do MPI stuff */
    MPI_Finalize();
    return 0;
}
```
MPI_THREAD_FUNNELED

- All MPI calls are made by the **master** thread
  - Outside the OpenMP parallel regions
  - In OpenMP master regions

```c
int buf[100];
int main(int argc, char ** argv)
{
  int provided;

  MPI_Init_thread(&argc, &argv,
                  MPI_THREAD_FUNNELED, &provided);
  if (provided < MPI_THREAD_FUNNELED)
    MPI_Abort(MPI_COMM_WORLD,1);

  for (i = 0; i < 100; i++)
    pthread_create(…,func,(void*)i);
  for (i = 0; i < 100; i++)
    pthread_join();

  void* func(void* arg) {
    int i = (int)arg;
    compute(buf[i]);
  }

  /* Do MPI stuff */

  MPI_Finalize();
  return 0;
}
```
MPI_THREAD_SERIALIZED

- Only **one** thread can make MPI calls at a time
  - Protected by OpenMP critical regions

```c
int buf[100];
int main(int argc, char ** argv)
{
    int provided;
    pthread_mutex_t mutex;

    MPI_Init_thread(&argc, &argv, MPI_THREAD_SERIALIZED, &provided);
    if (provided < MPI_THREAD_SERIALIZED)
        MPI_Abort(MPI_COMM_WORLD,1);

    for (i = 0; i < 100; i++)
        pthread_create(…,func,(void*)i);
    for (i = 0; i < 100; i++)
        pthread_join();

    MPI_Finalize();
    return 0;
}
```

```c
void* func(void* arg) {
    int i = (int)arg;
    compute(buf[i]);
    pthread_mutex_lock(&mutex);
    /* Do MPI stuff */
    pthread_mutex_unlock(&mutex);
}
```
**MPI_THREAD_MULTIPLE**

- **Any** thread can make MPI calls any time (restrictions apply)

```c
int buf[100];
int main(int argc, char ** argv)
{
    int provided;

    MPI_Init_thread(&argc, &argv,
                    MPI_THREAD_MULTIPLE, &provided);
    if (provided < MPI_THREAD_MULTIPLE)
        MPI_Abort(MPI_COMM_WORLD,1);

    for (i = 0; i < 100; i++)
        pthread_create(...,func,(void*)i);
    for (i = 0; i < 100; i++)
        pthread_join();

    MPI_Finalize();
    return 0;
}
```

```c
void* func(void* arg) {
    int i = (int)arg;
    compute(buf[i]);
    /* Do MPI stuff */
}
```
Threads and MPI

- An implementation is not required to support levels higher than MPI_THREAD_SINGLE; that is, an implementation is not required to be thread safe.
- A fully thread-safe implementation will support MPI_THREAD_MULTIPLE.
- A program that calls MPI_Init (instead of MPI_Init_thread) should assume that only MPI_THREAD_SINGLE is supported.
  - MPI Standard mandates MPI_THREAD_SINGLE for MPI_Init.
- A threaded MPI program that does not call MPI_Init_thread is an incorrect program (common user error we see).
MPI Semantics and MPI_THREAD_MULTIPLE

**Ordering:** When multiple threads make MPI calls concurrently, the outcome will be as if the calls executed sequentially in some (any) order

- Ordering is maintained within each thread
- User must ensure that collective operations on the same communicator, window, or file handle are correctly ordered among threads
  - E.g., cannot call a broadcast on one thread and a reduce on another thread on the same communicator
- It is the user's responsibility to prevent races when threads in the same application post conflicting MPI calls
  - E.g., accessing an info object from one thread and freeing it from another thread

**Progress:** Blocking MPI calls will block only the calling thread and will not prevent other threads from running or executing MPI functions
Ordering in MPI_THREAD_MULTIPLE: Incorrect Example with Collectives

### Process 0

- **Thread 0**: `MPI_Bcast(comm)`
- **Thread 1**: `MPI_Barrier(comm)`

### Process 1

- **Thread 0**: `MPI_Bcast(comm)`
- **Thread 1**: `MPI_Barrier(comm)`
Ordering in MPI_THREAD_MULTIPLE: Incorrect Example with Collectives

- P0 and P1 can have different orderings of Bcast and Barrier
- Here the user must use some kind of synchronization to ensure that either thread 1 or thread 2 gets scheduled first on both processes
- Otherwise a broadcast may get matched with a barrier on the same communicator, which is not allowed in MPI
Ordering in `MPI_THREAD_MULTIPLE`: Incorrect Example with Object Management

- The user has to make sure that one thread is not using an object while another thread is freeing it
  - This is essentially an ordering issue; the object might get freed before it is used
Blocking Calls in MPI_THREAD_MULTIPLE: Correct Example

- An implementation must ensure that the above example never deadlocks for any ordering of thread execution.
- That means the implementation cannot simply acquire a thread lock and block within an MPI function. It must release the lock to allow other threads to make progress.
The Current Situation

- All MPI implementations support MPI_THREAD_SINGLE
- They probably support MPI_THREAD_FUNNELED even if they don’t admit it.
  - Does require thread-safety for some system routines (e.g. malloc)
  - On most systems -pthread will guarantee it (OpenMP implies -pthread)
- Many (but not all) implementations support THREAD_MULTIPLE
  - Hard to implement efficiently though (thread synchronization issues)
- Bulk-synchronous OpenMP programs (loops parallelized with OpenMP, communication between loops) only need FUNNELED
  - So don’t need “thread-safe” MPI for many hybrid programs
  - But watch out for Amdahl’s Law!
Hybrid Programming: Correctness Requirements

- Hybrid programming with MPI+threads does not do much to reduce the complexity of thread programming
  - Your application still has to be a correct multi-threaded application
  - On top of that, you also need to make sure you are correctly following MPI semantics

- Many commercial debuggers offer support for debugging hybrid MPI+threads applications (mostly for MPI+Pthreads and MPI+OpenMP)
An Example we encountered

- We received a bug report about a very simple multithreaded MPI program that hangs.
- Run with 2 processes.
- Each process has 2 threads.
- Both threads communicate with threads on the other process as shown in the next slide.
- We spent several hours trying to debug MPICH before discovering that the bug is actually in the user’s program 😞.
if (rank == 1) {
    MPI_Send(NULL, 0, MPI_CHAR, 0, 0, MPI_COMM_WORLD);
    MPI_Send(NULL, 0, MPI_CHAR, 0, 0, MPI_COMM_WORLD);
    MPI_Recv(NULL, 0, MPI_CHAR, 0, 0, MPI_COMM_WORLD, &stat);
    MPI_Recv(NULL, 0, MPI_CHAR, 0, 0, MPI_COMM_WORLD, &stat);
    MPI_Send(NULL, 0, MPI_CHAR, 0, 0, MPI_COMM_WORLD);
    MPI_Send(NULL, 0, MPI_CHAR, 0, 0, MPI_COMM_WORLD);
    MPI_Recv(NULL, 0, MPI_CHAR, 0, 0, MPI_COMM_WORLD, &stat);
    MPI_Recv(NULL, 0, MPI_CHAR, 0, 0, MPI_COMM_WORLD, &stat);
} else {
    MPI_Recv(NULL, 0, MPI_CHAR, 1, 0, MPI_COMM_WORLD, &stat);
    MPI_Recv(NULL, 0, MPI_CHAR, 1, 0, MPI_COMM_WORLD, &stat);
    MPI_Send(NULL, 0, MPI_CHAR, 1, 0, MPI_COMM_WORLD);
    MPI_Send(NULL, 0, MPI_CHAR, 1, 0, MPI_COMM_WORLD);
    MPI_Recv(NULL, 0, MPI_CHAR, 1, 0, MPI_COMM_WORLD, &stat);
    MPI_Recv(NULL, 0, MPI_CHAR, 1, 0, MPI_COMM_WORLD, &stat);
    MPI_Send(NULL, 0, MPI_CHAR, 1, 0, MPI_COMM_WORLD);
    MPI_Send(NULL, 0, MPI_CHAR, 1, 0, MPI_COMM_WORLD);
}
Every send matches a receive on the other rank
Possible Ordering of Operations in Practice

- Because the MPI operations can be issued in an arbitrary order across threads, all threads could block in a RECV call.
MPI+OpenMP correctness semantics

- MPI only specifies interoperability with threads, not with OpenMP (or any other high-level programming model using threads)
  - OpenMP iterations need to be carefully mapped to which thread executes them (some schedules in OpenMP make this harder)
- For OpenMP tasks, the general model to use is that an OpenMP thread can execute one or more OpenMP tasks
  - An MPI blocking call should be assumed to block the entire OpenMP thread, so other tasks might not get executed
int main(int argc, char ** argv)
{
    MPI_Init_thread(NULL, NULL, MPI_THREAD_MULTIPLE, &provided);

    #pragma omp parallel for
    for (i = 0; i < 100; i++) {
        if (i % 2 == 0)
            MPI_Send(..., to_myself, ...);
        else
            MPI_Recv(..., from_myself, ...);
    }

    MPI_Finalize();

    return 0;
}

Iteration to OpenMP thread mapping needs to explicitly be handled by the user; otherwise, OpenMP threads might all issue the same operation and deadlock
Either explicit/careful mapping of iterations to threads, or using nonblocking versions of send/recv would solve this problem
OpenMP tasks: MPI blocking Calls (1/5)

```c
int main(int argc, char ** argv)
{
    MPI_Init_thread(NULL, NULL, MPI_THREAD_MULTIPLE, &provided);

#pragma omp parallel
{
    #pragma omp for
    for (i = 0; i < 100; i++) {
        #pragma omp task
        {
            if (i % 2 == 0)
                MPI_Send(..., to_myself, ..);
            else
                MPI_Recv(..., from_myself, ..);
        }
    }
}

MPI_Finalize();
return 0;
}
```

This can lead to deadlocks. No ordering or progress guarantees in OpenMP task scheduling should be assumed; a blocked task blocks its thread and tasks can be executed in any order.
int main(int argc, char ** argv)
{
    MPI_Init_thread(NULL, NULL, MPI_THREAD_MULTIPLE, &provided);

    #pragma omp parallel
    {
        #pragma omp taskloop
        for (i = 0; i < 100; i++) {
            if (i % 2 == 0)
                MPI_Send(..., to_myself, ..);
            else
                MPI_Recv(..., from_myself, ..)
        }
    }

    MPI_Finalize();
    return 0;
}
OpenMP tasks: MPI blocking Calls (3/5)

```c
int main(int argc, char ** argv)
{
    MPI_Init_thread(NULL, NULL, MPI_THREAD_MULTIPLE, &provided);

#pragma omp parallel
{
    #pragma omp taskloop
    for (i = 0; i < 100; i++) {
        MPI_Request req;
        if (i % 2 == 0)
            MPI_Isend(., to_myself, ., &req);
        else
            MPI_Irecv(., from_myself, ., &req);
        MPI_Wait(&req);
    }
}

MPI_Finalize();
return 0;
}
```

*Using nonblocking operations but with MPI_Wait inside the task region does not solve the problem*
int main(int argc, char ** argv)
{
    MPI_Init_thread(NULL, NULL, MPI_THREAD_MULTIPLE, &provided);

    #pragma omp parallel
    {
        #pragma omp taskloop
        for (i = 0; i < 100; i++) {
            MPI_Request req; int done = 0;
            if (i % 2 == 0)
                MPI_Isend(.., to_myself, .., &req);
            else
                MPI_Irecv(.., from_myself, .., &req);
            While (!done) {
                #pragma omp taskyield
                MPI_Test(&req, &done, ..);
            }
        }
    }

    MPI_Finalize();
    return 0;
}

Still incorrect; taskyield does not guarantee a task switch
int main(int argc, char ** argv)
{
   MPI_Init_thread(NULL, NULL, MPI_THREAD_MULTIPLE, &provided);
   MPI_Request req[100];

   #pragma omp parallel
   {
      #pragma omp taskloop
      for (i = 0; i < 100; i++)
      {
         if (i % 2 == 0)
            MPI_Isend(.., to_myself, .., &req[i]);
         else
            MPI_Irecv(.., from_myself, .., &req[i]);
      }
   }

   MPI_Waitall(100, req, ..);
   MPI_Finalize();
   return 0;
}

Correct example. Each task is nonblocking.
int main(int argc, char ** argv)
{
    /* Initialize MPI and RMA window */

#pragma omp parallel for
    for (i = 0; i < 100; i++) {
        target = rand();
        MPI_Win_lock(MPI_LOCK_EXCLUSIVE, target, 0, win);
        MPI_Put(..., win);
        MPI_Win_unlock(target, win);
    }

    /* Free MPI and RMA window */

    return 0;
}
Exercise 1: Stencil in Funneled mode (1/2)
Exercise 1: Stencil in Funneled mode (2/2)

- Parallelize computation (OpenMP parallel for)
- Main thread does all communication
- *Start from derived_datatype/stencil.c*
- *Solution available in threads/stencil_funneled.c*
Exercise 2: Stencil in Multiple mode (1/2)
Exercise 2: Stencil in Multiple mode (2/2)

- Divide the process memory among OpenMP threads
- Each thread responsible for communication and computation
- *Start from* threads/stencil_funneled.c
- *Solution available in* threads/stencil_multiple.c
Exercise 3: BSPMM in Funneled mode

- Parallelize dgemm computation (OpenMP parallel for)
- Main thread does all communication
- Start from rma/bspmm_counter.c
- Solution available in threads/bspmm_funneled.c
Exercise 4: BSPMM in Multiple mode

- Each thread queries the next available block multiplication
- Start from threads/bspmm_funneled.c
- Solution available in threads/bspmm_multiple.c
MPI+threads performance recommendations
Recommendation: Maximize independence between threads with communicators

- Each thread accesses to a **different communicator**
  - Each communicator may be associated with isolated resource in an MPI implementation

```c
MPI_Comm *comms;
int nthreads = omp_get_num_threads();
comms = malloc(sizeof(MPI_Comm) * nthreads);

for (i = 0; i < nthreads; i++)
    MPI_Comm_dup(MPI_COMM_WORLD, &comms[i]);

#pragma omp parallel
{
    int tid = omp_get_thread_num();
    #pragma omp taskloop
    for (i = 0; i < 100; i++)
        MPI_Isend(., comm[tid], &req[i]);
}
MPI_Waitall(100, req, .);
```
Recommendation: Maximize independence between threads with ranks or tags (1/2)

- Each thread communicates with **different peer_rank or tag**
  - MPI may assign isolated resource for different set of [peer_rank + tag]

```c
#pragma omp parallel
{
    int tid = omp_get_thread_num();
    #pragma omp taskloop
    for (i = 0; i < 100; i++)
        MPI_Isend(.., peer_ranks[tid], tid,
                    comm, &req[i]);
}
MPI_Waitall(100, req, ..);
```
Recommendation: Maximize independence between threads with ranks or tags (2/2)

- Threads have to match all receive messages in sequential (e.g., a single receive-queue) if a wildcard receive may be posted
  - Ensure ordering of message matching
- Let MPI know if you do not use wildcard receive
  - Info hints `mpi_assert_no_any_source`, `mpi_assert_no_any_tag` (already proposed to MPI standard)
  - MPI can get rid of the single receive-queue for the communicator

```c
MPI_Info info;
info = MPI_Info_create();
MPI_Info_set(info,
              "mpi_assert_no_any_source", "true");
MPI_Comm_set_info(comm, info);
MPI_Info_free(&info);
/* Communicate without ANY_SOURCE */
```
Communication Isolation Limitations

**Progress**: A blocked thread will not prevent progress of other runnable threads on the same process

- `ssend(comm1)` returns only after `irecv(comm1)` is posted
  - MPI may internally send handshake messages to synchronize
- Thread 0 has to make progress for comm1 in `wait(req0)` (e.g., access comm1’s receive-queue), to ensure `ssend(comm1)` can complete
Possible Optimizations MPI libraries can do

- Virtual Communication Interface (VCI)
  - Each VCI abstracts a set of network/shared-memory resources
  - Some networks support multiple VCIs: InfiniBand contexts, scalable endpoints over Intel Omni-Path
  - Traditional MPI implementation uses single VCI
    - Serializes all traffic
    - Does not fully exploit network hardware resources

- Utilizing multiple VCIs to maximize independence in communication
  - Separate VCIs per communicator or per RMA window
  - Distribute traffic between VCIs with respect to ranks, tags, and generally out-of-order communication
  - M-N mapping between Work-Queues and VCIs
Exercise 5: Stencil with Independent Communicators

- Divide the process memory among OpenMP threads
- Each thread responsible for communication and computation
- Each thread uses a different communicator
- Start from threads/stencil_multiple.c
- Solution available in threads/stencil_multiple_ncomms.c
Exercise 6: BSPMM with overlapping windows

- Each thread queries the next available block multiplication
- Each thread uses a different window (overlapped) for accessing A and B global matrices
  - Have to use a single window for C matrix and global counter in order to ensure atomicity
- Start from threads/bspmm_multiple.c
- Solution available in threads/bspmm_multiple_nwins.c
MPI+threads optimizations in Intel MPI 2019

- Supported starting Intel MPI Library 2019 (for Linux).
- `MPI_Init_thread(MPI_THREAD_MULTIPLE)`
- Environment variables
  - `I_MPI_THREAD_SPLIT=1`
  - `I_MPI_THREAD_RUNTIME=openmp`
- `MPI_THREAD_SPLIT`
  - Only threads with the same thread id can communicate using distinct communicators, limiting space of possible communication patterns.
- Known issues
  - Using `MPI_PROC_NULL` with `I_MPI_THREAD_SPLIT=1` causes errors.
  - `MPI_Finalize` can take long with `I_MPI_THREAD_SPLIT=1`.

For more information: https://software.intel.com/en-us/mpi-developer-guide-linux-multiple-endpoints-support
Exposing parallelism in micro-benchmarks

- All results, except “MPI_THREAD_MULTIPLE (multiple comms)” use Intel MPI 2019. The multiple comms version will be included into Intel MPI soon.
Exposing parallelism in stencil example

- Using 16 cores per node; 3 x 3 node grid.
- Halo exchange time of a rank on the central node.
- All results, except “MPI_THREAD_MULTIPLE (multiple comms)” use Intel MPI 2019. The multiple comms version will be included into Intel MPI soon.
Section Summary

- Hybrid MPI + “X” is a promising approach for large scale programming (e.g., MPI+Threads)
  - Less memory consumption
  - More efficient on-node data movement (load/store)
- MPI thread safety: SINGLE, FUNNELED, SERIALIZE, MULTIPLE
- Use MPI_Init_thread for threaded programs (i.e., not SINGLE)
- THREAD_MULTIPLE ordering & progress semantics
- Always maximize independence between threads in your program
  - Independent communicators, no wildcard, independent peer_ranks and tags
MPI Hybrid Programming: Accelerators

(Thanks to Jiri Kraus @ NVIDIA for several corrections and comments)
Introduction

Accelerators are becoming increasingly popular in parallel computing

- **CPUs**
  - Task-sequential execution model (focus on latency)
  - Small # of complex compute cores (out-of-order execution)
  - Deep pipelines
  - Large caches
  - Branch prediction hardware

- **GPUs**
  - Data-parallel execution model (focus on throughput)
  - Large # of simple compute elements (in-order execution)
  - Small caches
  - Shallow pipelines
  - Large off-chip global High-Bandwidth Memory (HBM)
  - High FLOPs/W and FLOPs/$
Top500 Accelerators Based Systems (June 2020)

- #2 - Summit (ORNL USA)
  - NVIDIA Tesla V100
- #3 - Sierra (LLNL USA)
  - NVIDIA Tesla V100
- #6 - HPC5 (Eni S.p.A Italy)
  - NVIDIA Tesla V100
- #7 - Selene (NVIDIA Corporation USA)
  - NVIDIA Tesla A100
- #9 - Marconi-100 (CINECA Italy)
  - NVIDIA Tesla V100
- #10 - Piz Daint (CSCS Switzerland)
  - NVIDIA Tesla P100
Upcoming Exascale Accelerators Based Systems

- **Aurora (ANL USA)**
  - Intel based technology

- **Frontier (ORNL USA)**
  - AMD based GPU technology

- **El Capitan (LLNL USA)**
  - AMD based GPU technology
Programming Model for Accelerators

- **GPUs** are well suited for fine grain data level parallelism
- Shared Memory, Single Instruction Multiple Data (SIMD) model
- Many available compute platforms and programming frameworks (focus on their memory model and interaction with MPI)
  - NVIDIA CUDA (NVIDIA platform only)
  - AMD ROCm & HIP
  - OpenMP
  - OpenACC (mentioned but not covered)
  - OpenCL & SYCL

(*)Single Program Multiple Data
Interoperability with MPI

**GPUs** have separate physical memory subsystem

_How to move data between GPUs with MPI?_

*Real answer:* It depends on what GPU library, what hardware and what MPI implementation you are using

*Simple answer:* For modern GPUs, “just like you would with a non-GPU machine”
Unified Virtual Addressing (UVA)

- UVA is a memory address management system supported in modern 64-bit architectures
  - Requires device driver support
- The same virtual address space is used for all processors, host or devices
- No distinction between host and device pointers
- The user can query the location of the data allocation given a pointer in the unified virtual address space and the appropriate GPU runtime library query APIs ("GPU-aware" MPI library)
Remote Direct Memory Access with UVA

- Only GPU-enabled MPI implementations can take advantage of UVA
- User can pass device pointer to MPI
- MPI implementation can query for the owner (host or device) of the data
- If the data is on the device, the MPI implementation can optimize data transfers
Intranode Communication with UVA

- Intranode Optimization
  - GPU peer-to-peer data transfers are possible
  - MPI can directly move data between GPU devices
Heterogeneous Memory Management (HMM)

- Next step towards the unification of heterogeneous memory spaces in the Linux Kernel (not yet available)
- Support started with version 4.14 through helper functions to be used by device drivers
  - Support paging in device for migrating memory between host and GPU
- Automatic data movement between host and GPU memories (called Unified Memory in CUDA)
  - Data is automatically migrated between host and GPU on page faults
  - Moving pages to GPU and back to host is similar to swap-out and swap-in of pages to and from disk

Single memory space accessible to all devices and host. Transparently managed heterogeneous memory.
MPI + HMM in a Nutshell

- In theory, any MPI implementation can transparently work with HMM
  - The MPI implementation can always assume that the data is on the host (or device)
  - GPUs take care of moving data between device and host memories
  - *Trying to register memory on the wrong device from the network should simply fail for HMM, but there have been reports of silent failures in this regard for CUDA, so you might need to be careful*
  - *Data in HMM can be corrupted if GPU updates pages during network transfer*

- In practice MPI implementations should never use HMM directly
  - Managed heterogeneous memory cannot be directly accessed by the network (**correctness issue**)
    - Virtual address cannot be pinned to a fixed physical memory region since GPU might need to migrate the data
    - Intermediate buffer is needed to copy data from HMM

- In any case MPI can never know in which device data is physically located
  - Data management is completely handled by GPU and can cause unnecessary data movement (**performance issue**)
MPI + HMM Assuming Data on Host

- MPI can assume data is on host memory
- MPI copies data to network pinned memory
  - Network registration will fail
- On a correct guess
  - The copy will not trigger a page fault to bring data from GPU
- On incorrect guess
  - An **expensive page fault** will occur
MPI + HMM Assuming Data on GPU

- MPI can assume data is on some GPU device memory
- MPI would need to move data from the GPU device memory to network pinned memory
  - This can be either host or GPU memory (but not unified memory)
- On a correct guess
  - The copy will not trigger a page fault
- On incorrect guess
  - An **expensive page fault** will occur when accessing data on the GPU device memory
- Most MPI implementations assume memory to reside on the GPU
Compute Unified Device Architecture (CUDA)

(Thanks to CJ Newburn from NVIDIA for review and comments)
Overview

- General-purpose parallel computing platform and programming model released by NVIDIA in 2006
- Provides a user library (libcuda), runtime (libcudart), device drivers and C/C++ compiler (NVCC)
- Programming language extensions for C/C++
  - Define C functions to run on the GPU (kernels) using the `__global__` declaration specifier
  - Kernels can be launched with different number of threads using the `<<<...>>>` execution syntax
  - Each thread executing the kernel is given a unique thread ID accessible from inside the kernel using the built-in `threadIdx` variable
- Support other languages such as FORTRAN

```c
/* Kernel definition */
__global__ void gpu_kernel(double *in, double *out)
{
    /* get indices from thread id */
    int i = threadIdx.x;
    int j = threadIdx.y;
    /* each thread performs work */
    out[i][j] = f(in, i, j);
}

int main()
{
    double *in_h, *out_h, *in_d, *out_d;
    in_h = malloc(size);
    out_h = malloc(size);
    cudaMemcpy(in_d, in_h, size, cudaMemcpyHostToDevice);
    cudaMemcpy(out_d, out_h, size, cudaMemcpyDeviceToHost);
    gpu_kernel<<<2,N>>>(in_d, out_d);
    cudaMemcpy(out_h, out_d, size, cudaMemcpyDeviceToHost);
    [...snip...]
    return 0;
}
```
**MPI + GPUDirect (CUDA ≥ 4)**

- GPUDirect 1.0 (Q2’ 2010) allows pinned memory to be shared by GPU and NIC such that GPU can directly copy data in/out pinned memory and NIC can DMA data from it.
- GPUDirect 2.0 (Peer-to-peer 2011) extends UVA support by allowing direct memory transfers between GPUs in the same node bypassing host completely.

```c
double *dev_buf;
cudaMalloc(&dev_buf, size);

if (my_rank == sender) {
    gpu_kernel<<<..>>>(dev_buf);
    MPI_Isend(dev_buf, size, MPI_DOUBLE, receiver, 0, comm, req);
} else {
    MPI_Recv(dev_buf, size, MPI_DOUBLE, sender, 0, comm, &status);
    gpu_kernel<<<..>>>(dev_buf);
}
```
MPI + GPUDirect RDMA (CUDA ≥ 5)

- Technology introduced in 2013 with Kepler-class GPUs and CUDA-5
- GPU memory is directly accessible to third-party devices, including network interfaces (NIC driver talks to CUDA driver to register GPU memory)
- RDMA operations to/from the device memory are possible and completely bypass the host memory (zero copy)

```c
double *dev_buf;
cudaMalloc(&dev_buf, size);
if (my_rank == sender) {
    gpu_kernel<<<..>>>(dev_buf);
    MPI_Isend(dev_buf, size, MPI_DOUBLE, receiver, 0, comm, req);
} else {
    MPI_Recv(dev_buf, size, MPI_DOUBLE, sender, 0, comm, &status);
    gpu_kernel<<<..>>>(dev_buf);
}
```

- Register memory to ensure CUDA memory operations complete before granting access to NIC:
  - cuPointerSetAttribute(…,CU_POINTER_ATTRIBUTE_SYNC_MEMOPS, …)
Unified Memory (UM) between host and device
- CUDA kernel driver has a copy of the page table of the host and can handle page faults by migrating pages from host to device & vice versa

UM-aware MPI implementations stage data into tmp buffer

As mentioned before, performance can be bad
- MPI never knows if pages are on host or device (can only guess)

```c
double *buf;
cudaMallocManaged(&buf, size);

/* initialize buf in host ... */

if (my_rank == sender) {
    gpu_kernel<<<..>>>(buf);
    MPI_Isend(buf, size, MPI_DOUBLE, receiver, 0, comm, req);
} else {
    MPI_Recv(buf, size, MPI_DOUBLE, sender, 0, comm, &status);
    gpu_kernel<<<..>>>(buf);
}
```
## MPI + CUDA Optimizations Historical Summary

<table>
<thead>
<tr>
<th>Period</th>
<th>CUDA version</th>
<th>Major Features</th>
<th>MPI Optimization Space</th>
<th>MPI Implementation Requirements</th>
</tr>
</thead>
</table>
| After 2011 | >= 4.0 < 5.0 | • GPUDirect 1.0: RDMA can use GPU pinned memory  
• GPUDirect 2.0: GPU peer-to-peer DMA possible | • Use DMA and RDMA without extra memory copies to temporary buffers  | GPU-aware MPI implementations                      |
| After 2012 | >= 5.0       | • GPUDirect RDMA: GPU memory is directly accessible to third-party devices     | • Completely bypass host memory through RDMA to/from GPU memory                        | GPU-aware MPI implementations                      |
| After 2014 | >= 6.0       | • Unified Memory: shared memory between host and devices and automatic page migration | • The hardware takes care of moving data between host and device memories  
• MPI optimizations are limited and need user hints | GPU-aware MPI implementations needed for performance |
MPI + GPUDirect RDMA (Supported HW & SW)

- Mellanox Host Channel Adapters (HCA):
  - ConnectX-3, ConnectX-3 Pro, Connect IB, ConnectX-4, ConnectX-5
  - MLNX_OFED v2.1-x.x.x or later
  - Plugin Module to enable GPUDirect RDMA

- NVIDIA GPUs:
  - NVIDIA Tesla, Quadro K-Series or Tesla/Quadro P-Series
  - NVIDIA Driver
  - NVIDIA Runtime and Toolkit
Summary

- Accelerators are becoming increasingly important in HPC
- MPI is playing its role in enabling the usage of accelerators across distributed memory nodes
- The situation with MPI + GPU support is improving in both MPI implementations and in GPU hardware/software
  - For CUDA and ROCm P2P/RDMA support from GPU memory is enabled for contiguous datatypes through the UCX driver
  - For OpenCL/SYCL SVM can potentially enable similar optimizations as CUDA/ROCm but at the current state no such support is available and explicit data movement between host and device memory is still required
  - For OpenMP/OpenACC data movement is managed through directives but compilers can decide to leverage HMM
Exercise: Stencil with GPU

- Use GPU for updating the grid
  - Compute the grid on GPU
  - Pack/Unpack Halo regions to host memory for communication
- Start from accelerators/stencil_cuda_copy.c
- Solution available in accelerators/stencil_cuda_direct.c
- Special Environment Setup
  
  For stencil_cuda_copy.c
  +mvapich2
  +cuda-10.0

  For stencil_cuda_direct.c
  +mvapich2-2.3.4-cuda10.0
  +cuda-10.0
Concluding Remarks

- Parallelism is critical today, given that that is the only way to achieve performance improvement with the modern hardware
- MPI is an industry standard model for parallel programming
  - A large number of implementations of MPI exist (both commercial and public domain)
  - Virtually every system in the world supports MPI
- Gives user explicit control on data management
- Widely used by many scientific applications with great success
- Your application can be next!
Web Pointers

- MPI standard: [http://www.mpi-forum.org/docs/docs.html](http://www.mpi-forum.org/docs/docs.html)

- MPI implementations:
  - MPICH: [http://www.mpich.org](http://www.mpich.org)
  - MVAPICH: [http://mvapich.cse.ohio-state.edu/](http://mvapich.cse.ohio-state.edu/)
  - Open MPI: [http://www.open-mpi.org/](http://www.open-mpi.org/)
  - IBM MPI, Cray MPI, HP MPI, TH MPI, ...

- Several MPI tutorials can be found on the web
Tutorial Books on MPI

Basic MPI

Using MPI
Portable Parallel Programming with the Message-Passing Interface
third edition

William Gropp
Ewing Lusk
Anthony Skjellum

Advanced MPI, including MPI-3

Using Advanced MPI
Modern Features of the Message-Passing Interface

William Gropp
Torsten Hoefler
Rajeev Thakur
Ewing Lusk
Book on Parallel Programming Models

Edited by Pavan Balaji

- **MPI**: W. Gropp and R. Thakur
- **GASNet**: P. Hargrove
- **OpenSHMEM**: J. Kuehn and S. Poole
- **UPC**: K. Yelick and Y. Zheng
- **Global Arrays**: S. Krishnamoorthy, J. Daily, A. Vishnu, and B. Palmer
- **Chapel**: B. Chamberlain
- **Charm++**: L. Kale, N. Jain, and J. Lifflander
- **ADLB**: E. Lusk, R. Butler, and S. Pieper
- **Scioto**: J. Dinan
- **SWIFT**: T. Armstrong, J. M. Wozniak, M. Wilde, and I. Foster
- **CnC**: K. Knobe, M. Burke, and F. Schlimbach
- **OpenMP**: B. Chapman, D. Eachempati, and S. Chandrasekaran
- **Cilk Plus**: A. Robison and C. Leiserson
- **Intel TBB**: A. Kukanov
- **CUDA**: W. Hwu and D. Kirk
- **OpenCL**: T. Mattson
MPI for Scalable Computing

Tutorial at ATPESC, July 2020

Latest slides and code examples are available at

https://anl.box.com/v/atpesc20-mpi-tutorial

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